

# Verification of Embedded Software from Mars to Actions

Charles Pecheur, UC Louvain  
(formerly RIACS / NASA Ames)



From Mars ...



## ... to Actions

```
MODULE agent
```

```
  IVAR move : boolean;
```

```
  VAR count : 0..10;
```

```
  ASSIGN
```

```
    init(count) := 0 ;
```

```
    next(count) := case
```

```
      move & count < 10: count + 1;
```

```
      1 : count;
```

```
    esac;
```

```
  DEFINE win := (count=10);
```

```
MODULE main
```

```
  VAR alice : agent;
```

```
  VAR bob : agent;
```

```
SPEC !EAX (bob.move) bob.count = 0
```

```
SPEC AAX (bob.move & alice.move) (bob.count > 0 & alice.count > 0)
```

```
SPEC AAF (bob.move) bob.win
```

# Outline

## Model-Based Autonomy and Diagnosis

Verification of Model-Based Controllers

Verification of Diagnosability

Symbolic Verification with Knowledge

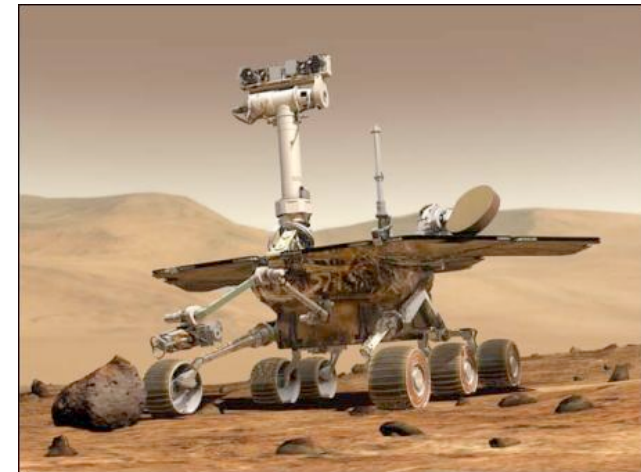
Symbolic Verification with Actions

Conclusions

# Autonomy (at NASA)

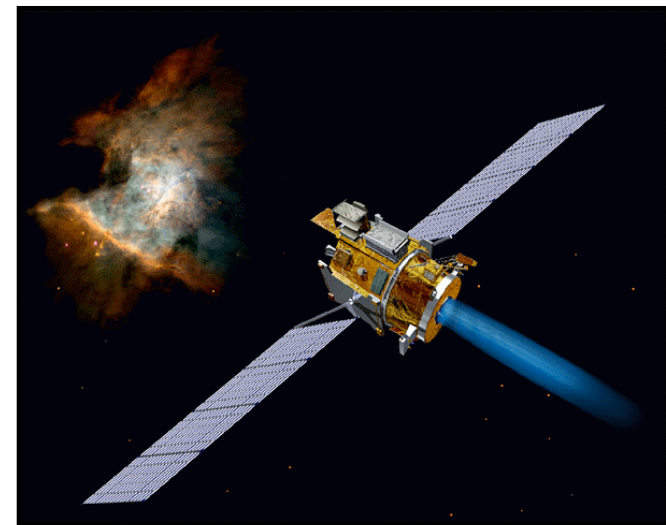
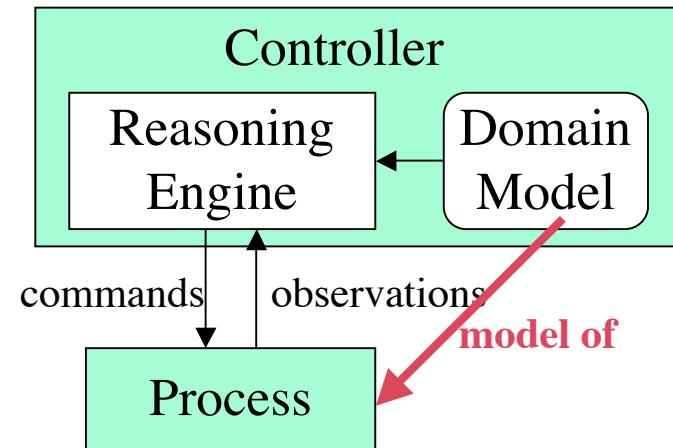
**Autonomous spacecraft = on-board intelligence (= AI)**

- **Goal:** Unattended operation in an unpredictable environment
- **Approach:** **model-based reasoning**
- **Pros:** smaller mission control crews, no communication delays/blackouts
- **Cons:** **Verification and Validation ???**  
Much more complex, huge state space
- **Better verification is critical for adoption**



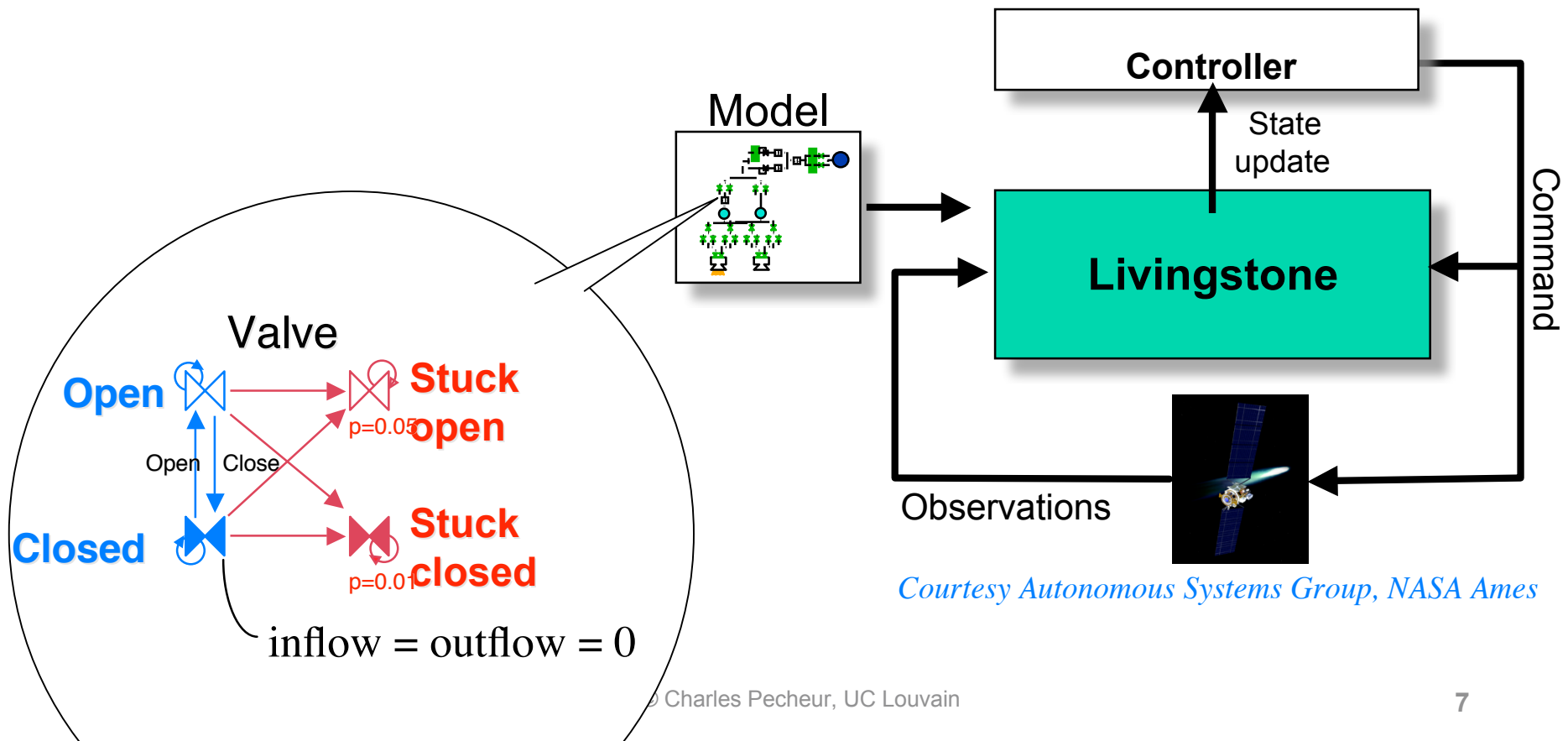
# Model-Based Autonomy

- Based on AI technology
- Generic **reasoning engine** + application-specific **model**
- Model describes (normal and faulty) behaviour of the process
- Engine selects control actions "on-the-fly" based on the model
  - ... rather than pre-coded decision rules
  - better able to respond to unanticipated situations

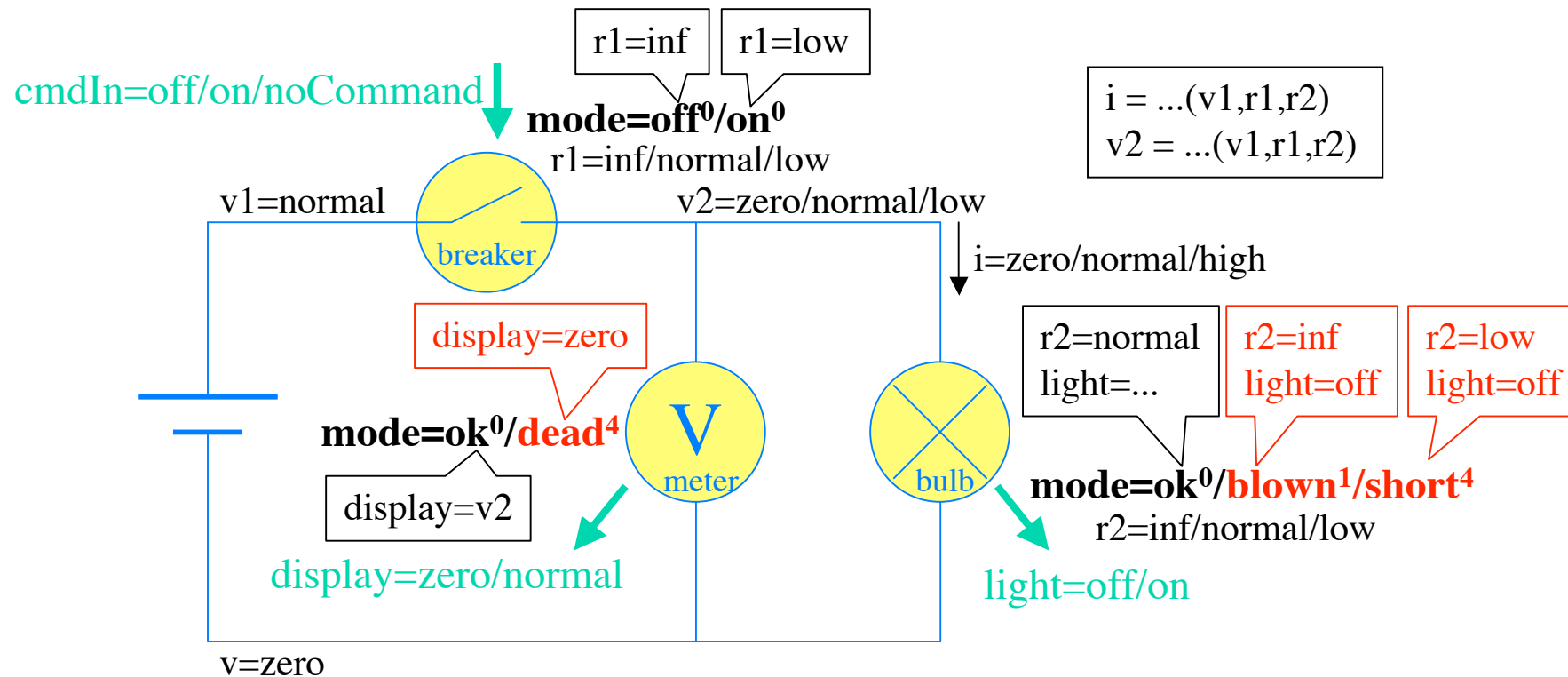


# Livingstone

- Model-based diagnosis system from NASA Ames
  - i.e. an advanced state estimator
- Uses a discrete, qualitative model to reason about faults
  - => naturally amenable to formal analysis



# A Simple Livingstone Model



Goal: determine **modes** from **observations**  
Generates and tracks *candidates*

breaker	bulb	meter	rank
off <sup>0</sup>	ok <sup>0</sup>	ok <sup>0</sup>	0
off <sup>0</sup>	ok <sup>0</sup>	blown <sup>1</sup>	1
on <sup>0</sup>	dead <sup>4</sup>	short <sup>4</sup>	8



# Outline

Model-Based Autonomy and Diagnosis

**Verification of Model-Based Controllers**

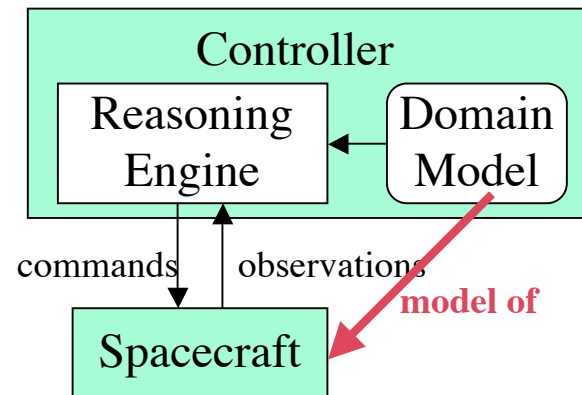
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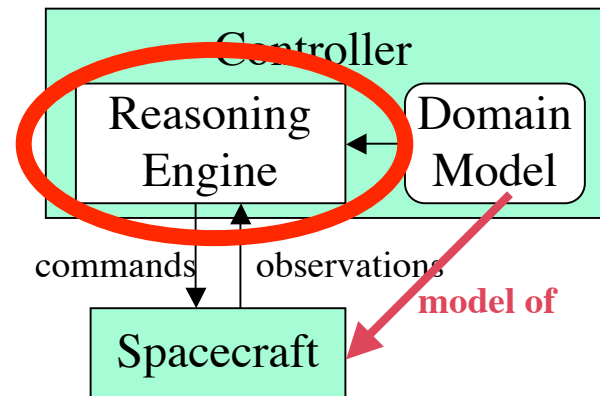
# Verify Model-Based Control?



Of course, but what exactly?

- The model?
- The engine?
- The whole controller?
- **All of the above!**

# Verification of the Engine

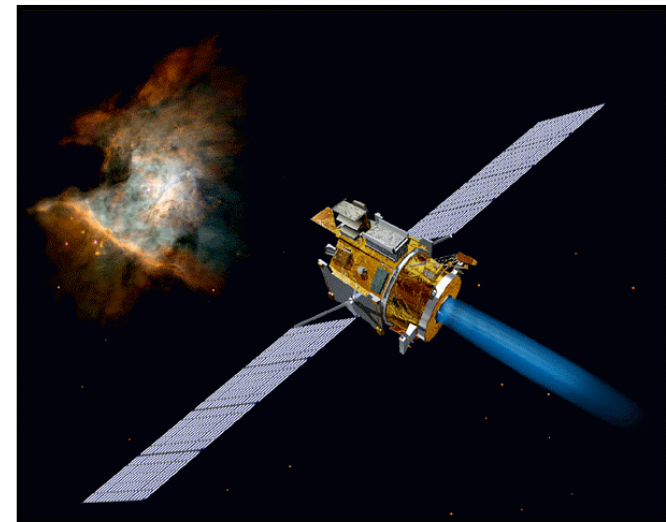


- A (technically complex) computer program
  - Use traditional software verification approaches
  - Maybe full-blown proof on core algorithms
- Generic, re-used across applications
  - More likely to be stable and trustable
  - Like compilers, interpreters, virtual machines, etc

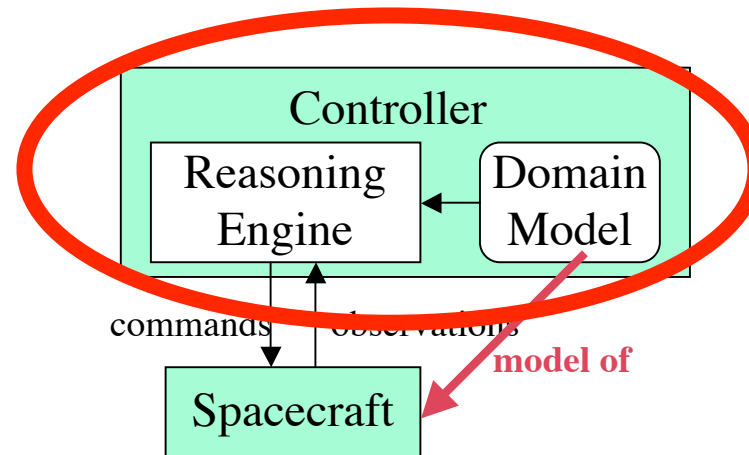
# The RAX Bug

## Remote Agent Experiment (1999)

- **cause** : missing critical section in concurrent program
- **effect** : race condition and deadlock in flight
  - in supervised experiment, no mission damage
- **solution** : model checking
  - a similar bug was found before flight using SPIN on another part of the code
  - See [Havelund et al. 2000]



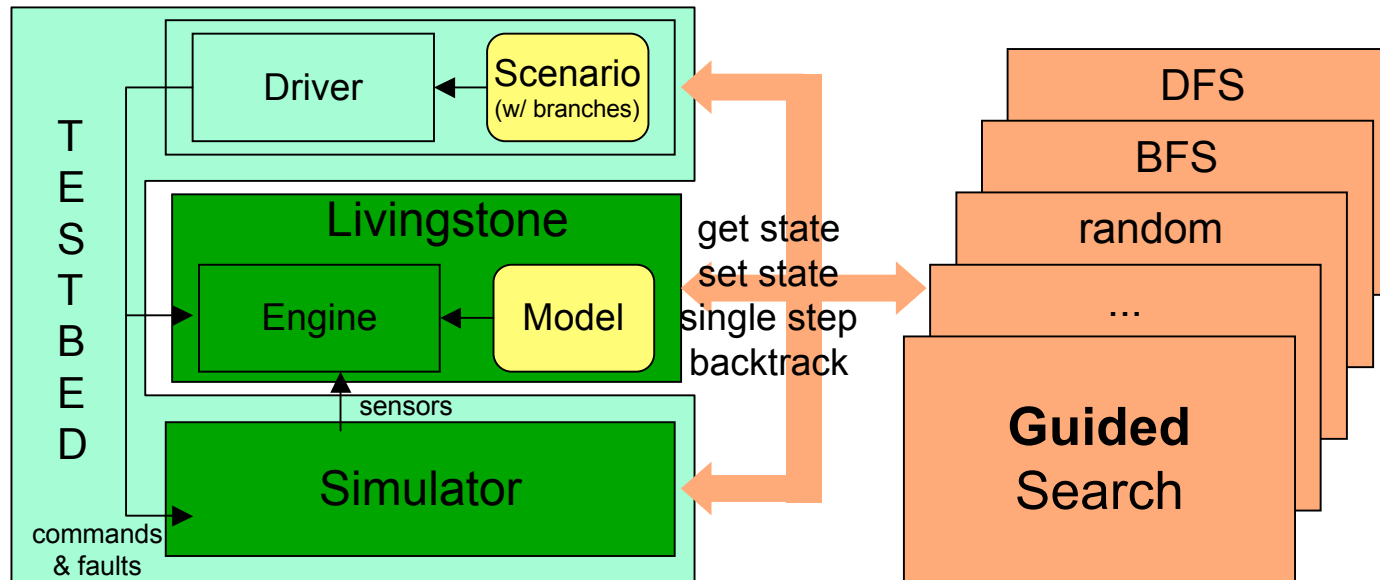
# Verification of the Controller



- good model + good engine  $\neq$  good controller
  - Heuristics in engine, simplifications in model
- System-level verification
  - Controller as black (or grey) box
  - Need a model of the environment (test harness)
  - Applicable to others than model-based

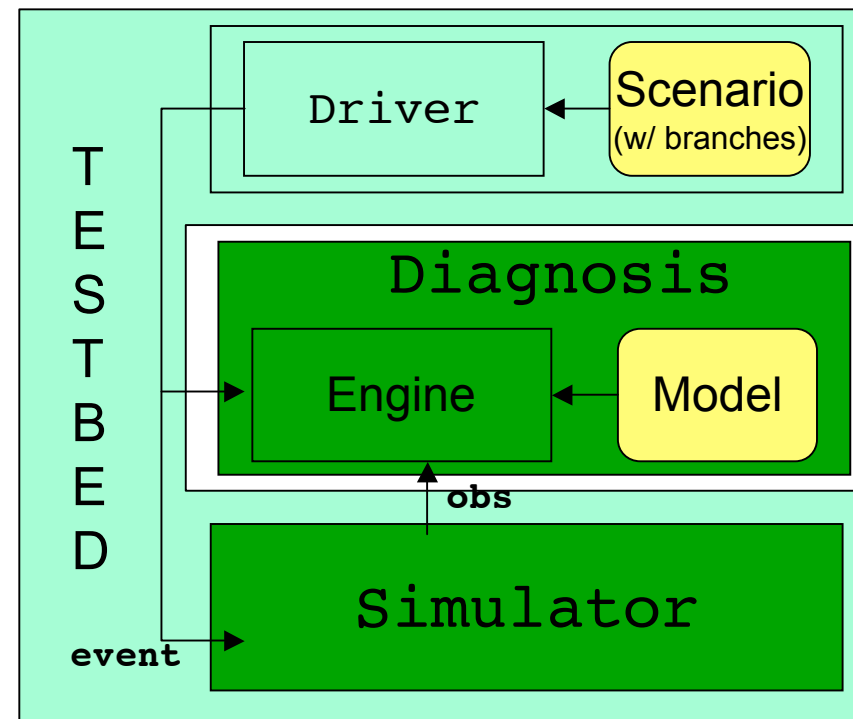
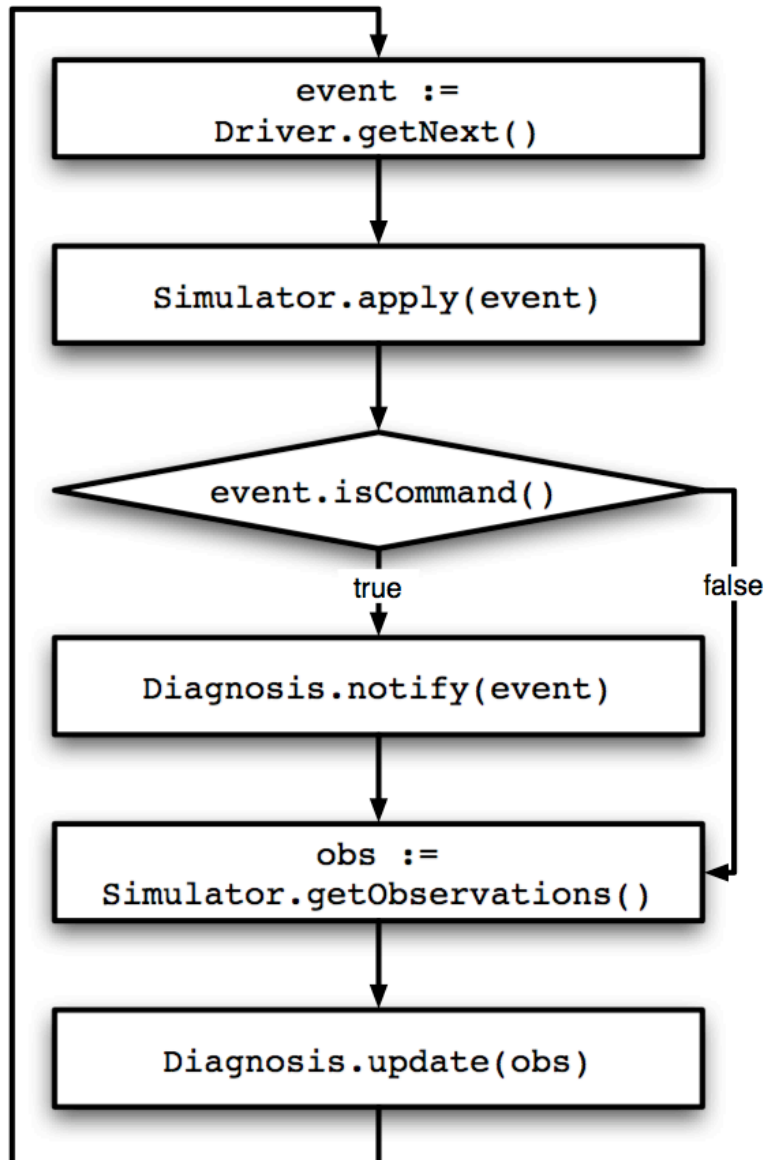
# Livingstone PathFinder

with Tony Lindsey (QSS / NASA Ames)



- An advanced testing/simulation framework for Livingstone applications
  - Executes the **Real Livingstone Program** in a simulated environment (testbed)
  - **Instrument** the code to be able to **backtrack** between alternate paths
- **Modular** architecture with generic APIs (in Java)
  - allows different diagnosers, simulators, search algorithms and strategies, error conditions, ...
- See TACAS'04 paper

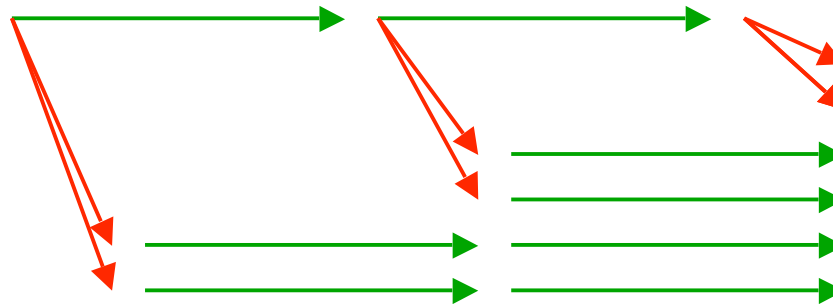
# One Diagnosis Step



# LPF Scenario Example

```

mix {
  "command test.sv02.valveCmdIn=close";
  "command test.sv02.valveCmdIn=open";
  ...
} and {
  choose
    "fault test.forwardLO2.mode=unknownFault"; or
    "fault test.mpre101p.mode=faulty"; or
    ...
}
  
```

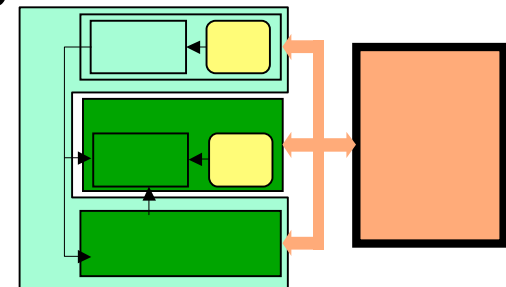


- Sequence of commands || choice of faults
- "default" scenario, can be generated automatically

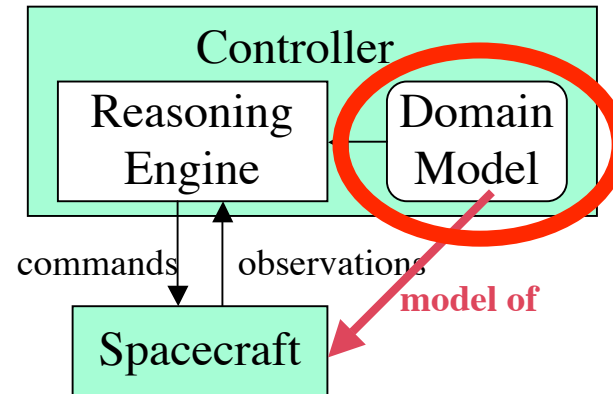


# LPF Search

- The whole testbed is seen as a transition system
- API to enumerate transitions, backtrack, get/set state
  - Shared with Java PathFinder (v.2)<sup>[Visser et al. 00]</sup>
  - Principle inspired from OPEN/CAESAR<sup>[Garavel 98]</sup>
- Search engine fixes exploration strategy
  - Depth-First
  - Breadth-First
  - **Heuristic**
  - Others are possible (random, pattern-based, interactive)
- + Halting conditions (for any strategy)
  - Find first / all / shortest error trace(s)



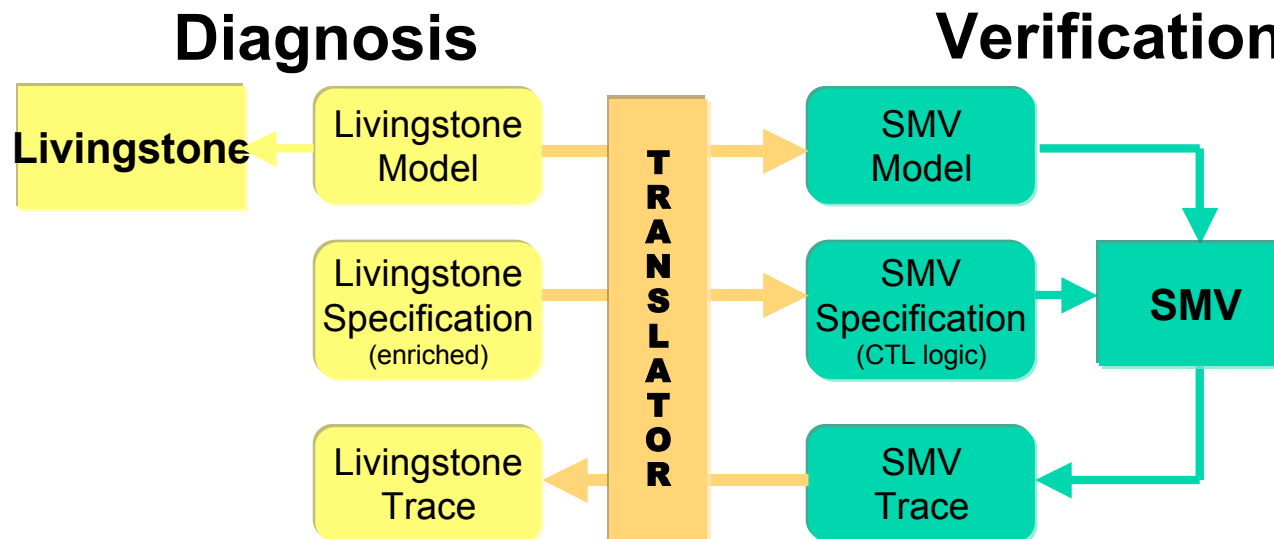
# Verification of the Model



- This is the "application code"
  - where the development effort (and bugs) are
- Abstract, concise, amenable to formal analysis
  - this is another benefit of model-based approaches
  - ... or model-based design in general
- Use **symbolic model checking**

# Livingstone-to-SMV Translator

*Joint work with Reid Simmons (Carnegie Mellon)*

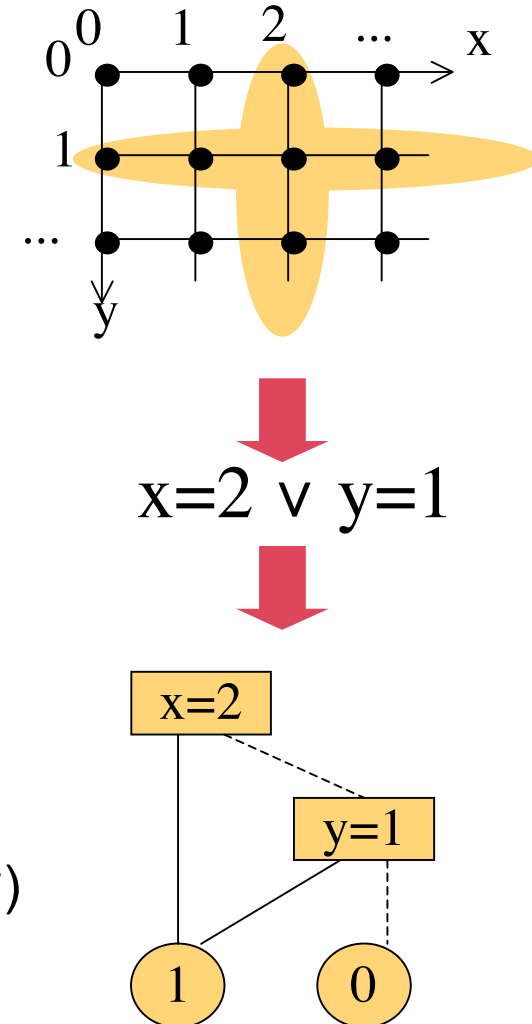


- A translator that converts Livingstone models, specs, traces to/from SMV (in Java)
  - SMV: symbolic model checker (both BDD and SAT-based) allows exhaustive analysis of very large state spaces ( $10^{50+}$ )
- Hides away SMV, offers a **model checker for Livingstone**
- Enriched specification syntax (vs. SMV's core temporal logic)
- Graphical interface, integration in Livingstone development tools

# SMV / NuSMV

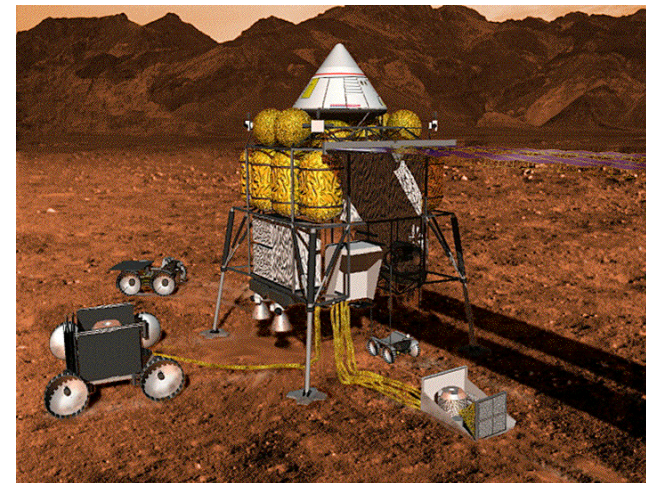
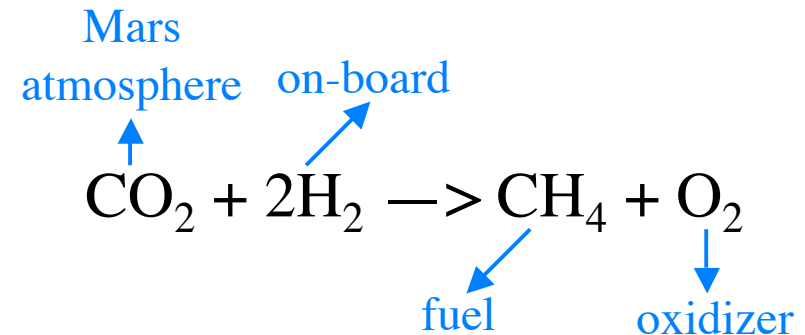
Mainstream **symbolic** model checker

- Original SMV from Carnegie Mellon, currently NuSMV from IRST (and Cadence SMV)
- Rich modeling **language**
- Many **features and options**
- Uses **symbolic** computation over **boolean** encoding
  - using BDDs or SAT (bounded)
  - finite models
  - Can handle **very large state spaces** ( $10^{50+}$ )



# In-Situ Propellant Production

- Use atmosphere from Mars to make fuel for return flight.
- Livingstone controller developed at NASA KSC.
- Components are tanks, reactors, valves, sensors...
- Exposed improper flow modeling.
- Latest model is  $10^{50}$  states.



# Verification of Diagnosis Models

- Coding Errors
  - e.g. Consistency, well-defined transitions, ...
  - Generic
  - Compare to Lint for C
- Model Correctness
  - Expected properties of modeled system
  - e.g. flow conservation, operational scenarios, ...
  - Application-specific
- **Diagnosability**
  - Are faults detectable/diagnosable?
    - Given available sensors
    - In all/specific operational situations (dynamic)

# Outline

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Verification of Model-Based Controllers

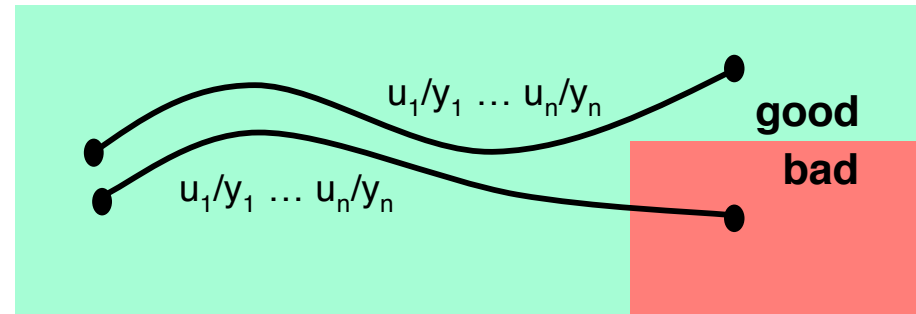
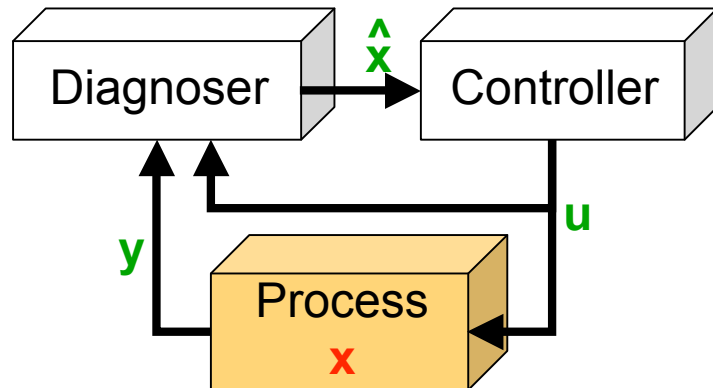
**Verification of Diagnosability**

Symbolic Verification with Knowledge

Symbolic Verification with Actions

Conclusions

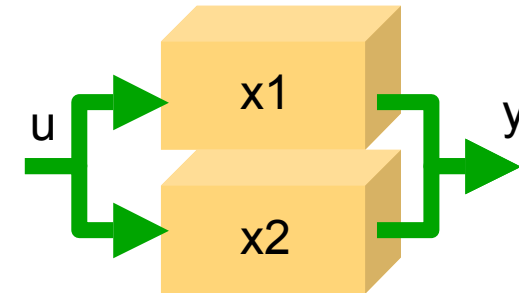
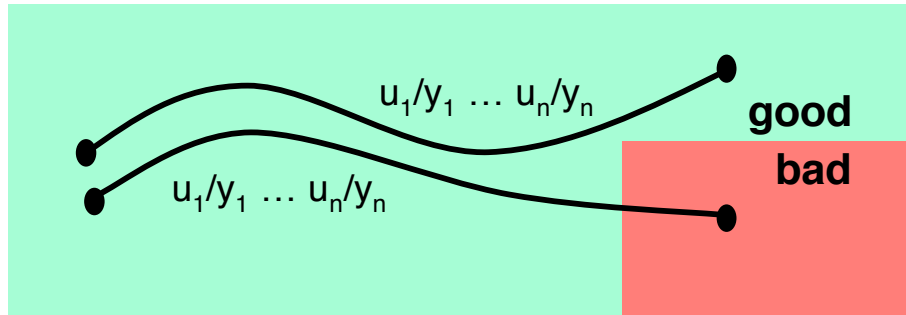
# Diagnosability



- **Diagnosis:** estimate the hidden state  $x$  (incl. failures) given observable commands  $u$  and sensors  $y$ .
- **Diagnosability:** Can (a smart enough) *Diagnoser* always tell when *Process* comes to a **bad** state?
- **Property of the Process** (not the Diagnoser)
  - even for non-model-based diagnosers
  - but analysis needs a (process) model



# Verification of Diagnosability



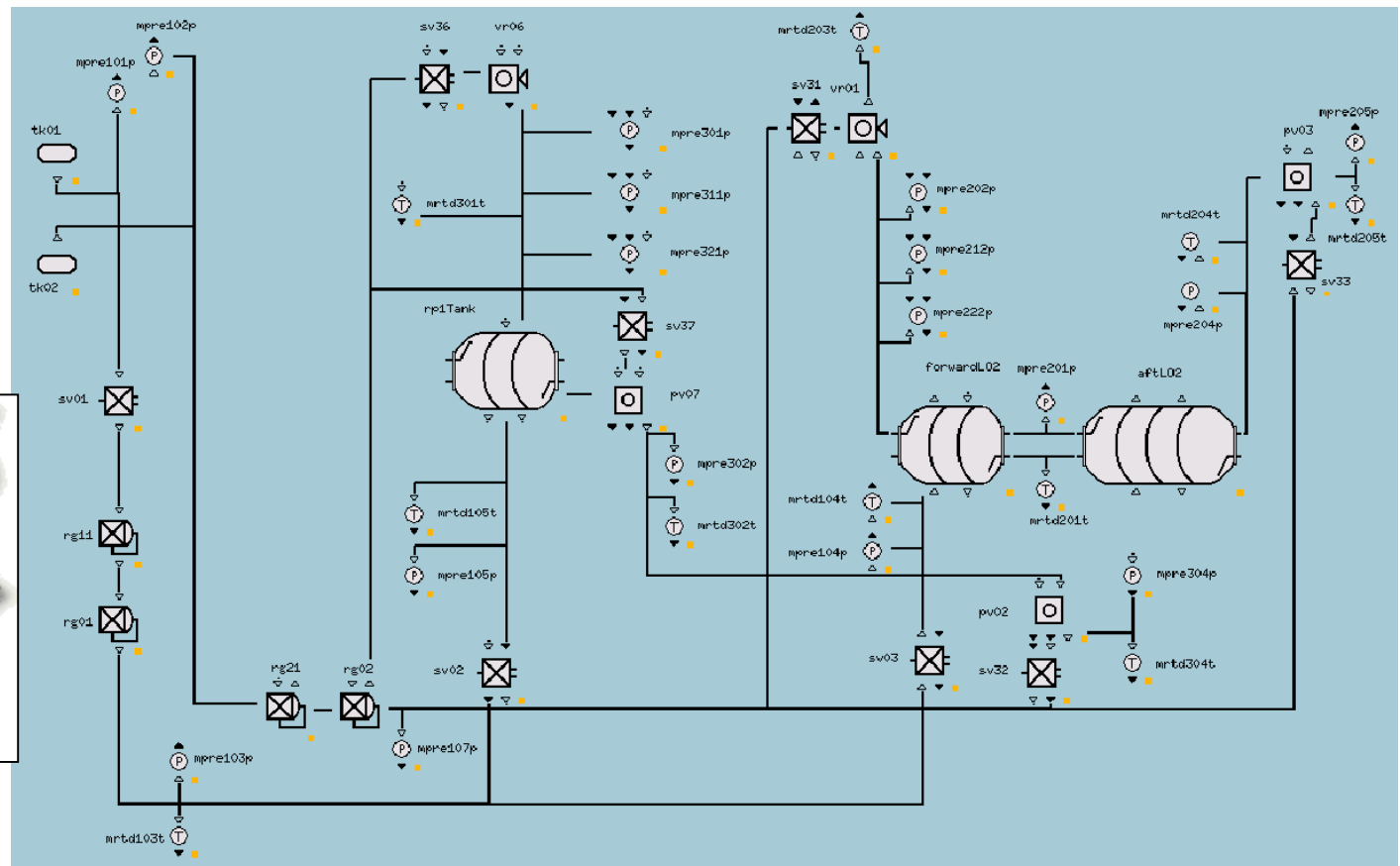
- **Intuition:** **bad** is diagnosable if and only if there is no pair of trajectories, one reaching a **bad** state, the other reaching a **good** state, with identical observations.
  - or some generalization of that: (context, two different faults, ...)
- **Principle:**
  - consider two concurrent copies  $x1$ ,  $x2$  of the process, with coupled inputs  $u$  and outputs  $y$
  - check for reachability of (**good**( $x1$ ) && **bad**( $x2$ ))
- Back to a classical (symbolic) model checking problem !
- Supported by Livingstone-to-SMV translator

# X-34 / PITEX

- Propulsion IVHM Technology Experiment (ARC, GRC)
- Livingstone applied to propulsion feed system of space vehicle
- Livingstone model is  $4 \cdot 10^{33}$  states



FMICS 07, 1 June 2007



# PITEX Diagnosability Error

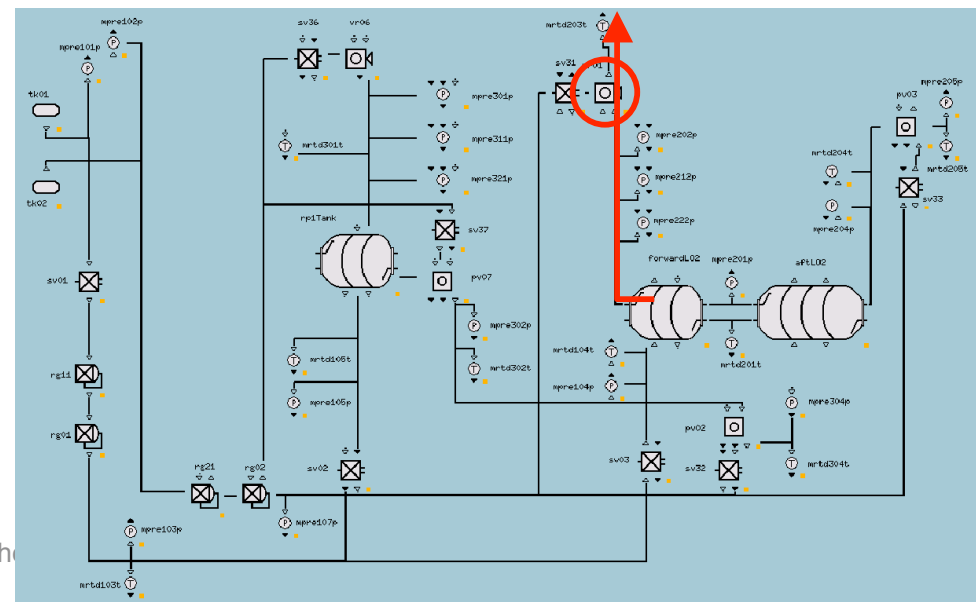
*with Roberto Cavada (IRST, NuSMV developer)*

- "Diagnosis can decide whether the venting valve VR01 is closed or stuck open (assuming no other failures)"

**INVAR !test.multibroken() & twin(!test.broken())**

**VERIFY INVARIANT !(test.vr01.mode=stuckOpen & twin(test.vr01.valvePosition=closed))**

- Results show a pair of traces with same observations, one leading to **VR01 stuck open**, the other to **VR01 closed**. Application specialists fixed their model.



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Symbolic Verification with Actions

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# Epistemic Logic

- Reasoning about knowledge
  - $K_a \varphi$  = agent  $a$  **knows**  $\varphi$
- Interpreted over an **Interpreted System (IS)**
  - **Transition system**  $T$  +
  - **Observation functions**  $obs_a(\sigma)$  over runs  $\sigma$  of  $T$
  - $K_a \varphi$  holds after  $\sigma$  iff  $\varphi$  holds after all  $\sigma'$  such that  $obs_a(\sigma) = obs_a(\sigma')$
- **CTLK** = **temporal + epistemic** logic

# Observation Function

- **In general** : agents reason about “everything they have seen so far” (total recall)
  - $\text{obs}_a(\sigma)$  over **runs**  $\sigma$
  - memory built into the logic
  - model checking hard to undecidable
- **Observational view** : agents reason about the current state only
  - $\text{obs}_a(s)$  over **states**  $s$
  - memory explicit in the model
  - **symbolic model checking** can be generalized from CTL to CTLK

# Diagnosability and CTLK

*joint work with Franco Raimondi (UC London)*

Considering the diagnoser as an agent  $D$  observing the system,

Fault  $F$  is diagnosable

iff

$$AG (K_D F \vee K_D \sim F)$$

- **Diagnosability** can be framed as a **temporal epistemic** model-checking problem
- **Caveat** : general diagnosability requires total recall
  - or explicit (bounded) memory of observations

# From CMAS to SMV

- CMAS : symbolic model checker for CTLK
  - developed by Franco Raimondi
  - BDD-based
  - Good performance but very crude modelling language
- Could we do CTLK in NuSMV?
  - Leverage SMV's rich modelling language
  - Re-use models generated from Livingstone
- Need a reduction from CTLK to (enhanced?) CTL



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# From Knowledge to Actions

- The observation function  $\text{obs}_a(s)$  induces an **accessibility** (equivalence) **relation**  $\sim_a$  over reachable states  $s$ 

$$s \sim_a s' \text{ iff } \text{obs}_a(s) = \text{obs}_a(s')$$
- An **interpreted system** is a Kripke structure with several transition relations  $\rightarrow, \sim_{a1}, \dots, \sim_{an}$
- Or equivalently, a **labelled transition system** (LTS) over an action alphabet  $\{t, a1, \dots, an\}$
- **Corresponding reduction of CTLK?**

# Action-Based Logics

- Large body of published work in **action-based temporal logics** (applicable to LTS)
  - ACTL [deNicola-Vaandrager], ACTL\*, Hennessy-Milner, etc.
  - Do not quite fit our purpose
  - No (well-known?) symbolic model-checker

# Action-Restricted CTL (ARCTL)

- Variant of ACTL
- Action conditions  $\alpha$  on path quantifiers
  - e.g.  $\mathbf{A}_\alpha \mathbf{F} \varphi$  = on all  $\alpha$ -paths, sooner or later  $\varphi$ 
    - vs. on temporal quantifiers in ACTL
      - e.g.  $\mathbf{A} \mathbf{F}_\alpha \varphi$  = on all paths, there is an  $\alpha$ -prefix to  $\varphi$
- $\alpha$ -restricted formula on full model =  
unrestricted formula on  $\alpha$ -restricted model
- (IS sat CTLK) can be reduced to (LTS sat ARCTL)
  - needs reachability = reverse temporal transitions

# Symbolic Model-Checking for Action-Based Logics

- Classical symbolic model-checking for CTL generalizes naturally to ARCTL or ACTL
  - some subtleties due to finite  $\alpha$ -paths and fairness

$$eax(A, S) = \{s \mid \exists a, s' \cdot s \xrightarrow{a} s' \wedge a \in A \wedge s' \in S\}$$

$$eau(A, S, S') = \mu Z \cdot S' \cup (S \cap eax(A, Z))$$

$$eag(A, S) = \nu Z \cdot S \cap eax(A, Z)$$

- NuSMV already has “actions” in models
  - called input variables (IVARs)
  - but not allowed in CTL

# Action-Based Logics in NuSMV

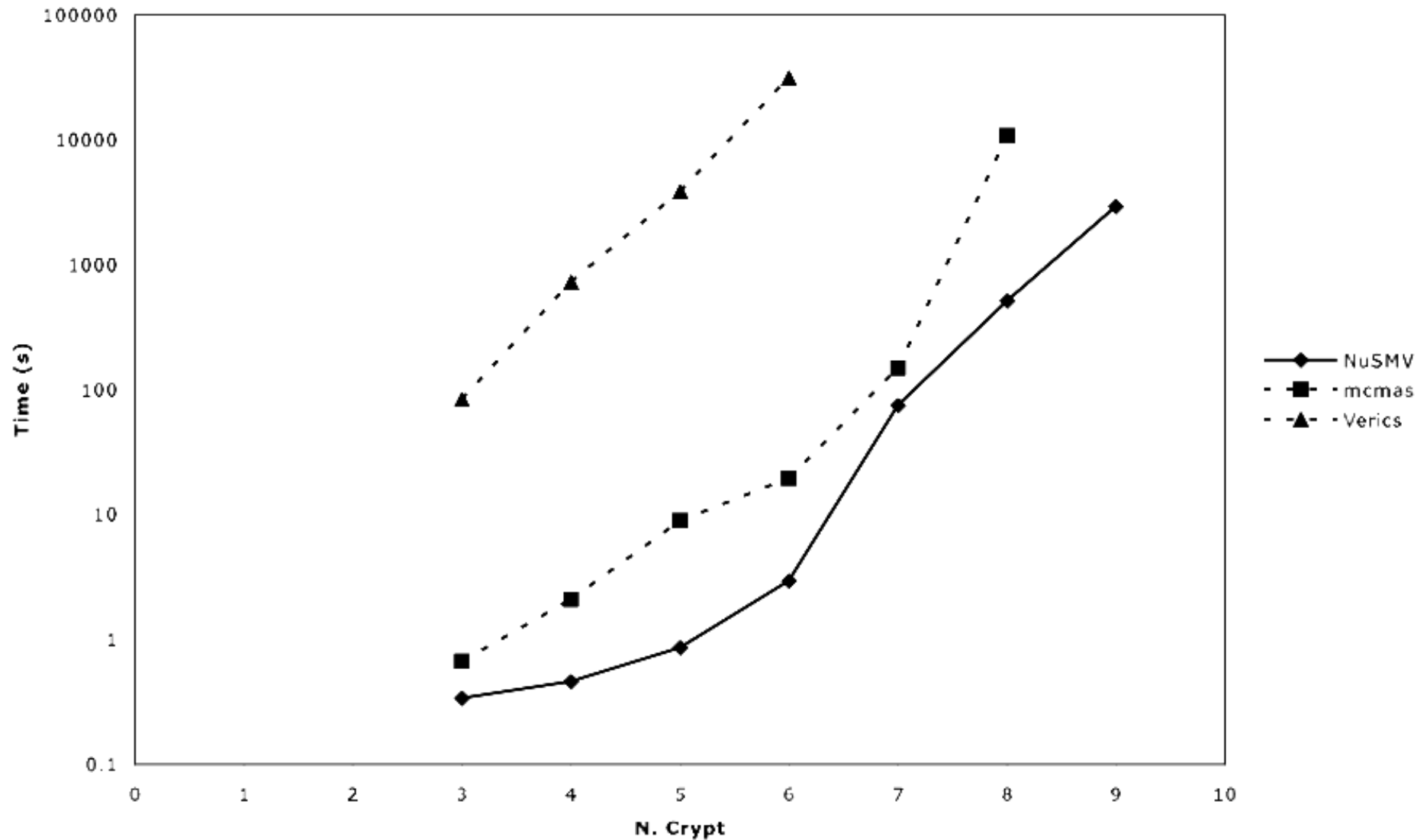
We added ARCTL support to NuSMV

- V1: reduction to KS + CTL,  
projecting actions into post-states  
e.g.  $\mathbf{A}_\alpha \mathbf{X} \varphi$  reduces to  $\mathbf{AX} (\alpha \Rightarrow \varphi) \wedge \mathbf{EX} \alpha$
- V2: native ARCTL support, using IVARs
- see [Pecheur-Raimondi 2006]

## CTLK in NuSMV

- CTLK and agents (observed variables) handled by a macro package (m4)
- Good performance wrt. dedicated model checkers (CMAS, Verics), see next slide
- see [Raimondi-Pecheur-Lomuscio 2005]

# CTLK on Dining Cryptographers





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# Summary: From Mars to Actions

Deep-space missions (incl. **Mars**)

=> Model-based autonomy (incl. diagnosis)

=> **Model-based verification**

=> **Diagnosability**

=> **Epistemic Logics**

=> **Logics with Actions**

# Lessons Learned

- Verification of **model-based controllers**
  - **Needs** advanced verification (because of large state space)
  - **Facilitates** advanced verification (thanks to model)
- Verification of **control software**
  - Control loop, observability/commandability
    - In particular, failure diagnosability and recoverability
  - Leads to epistemic, action logics
- **Model checking**
  - Applicable to these problems
  - symbolic model checking saves the day
- Verification of **software**
  - All other principles still apply: process, testing, ...

# Perspectives

- Key ideas:
  - **model-based analysis (model checking)**
  - **partial observability**
- Extensions
  - from discrete to continuous, real-time, **hybrid models**
  - from fault diagnosis to **planning**
    - e.g. test-case generation for planners  
see [Raimondi-Pecheur-Brat 2007]
- Connections
  - with classical **risk analysis** (fault trees, FMEA)
  - with **man-machine interface** issues (observability!)
  - with **game theory** (the Controller vs. the Environment)

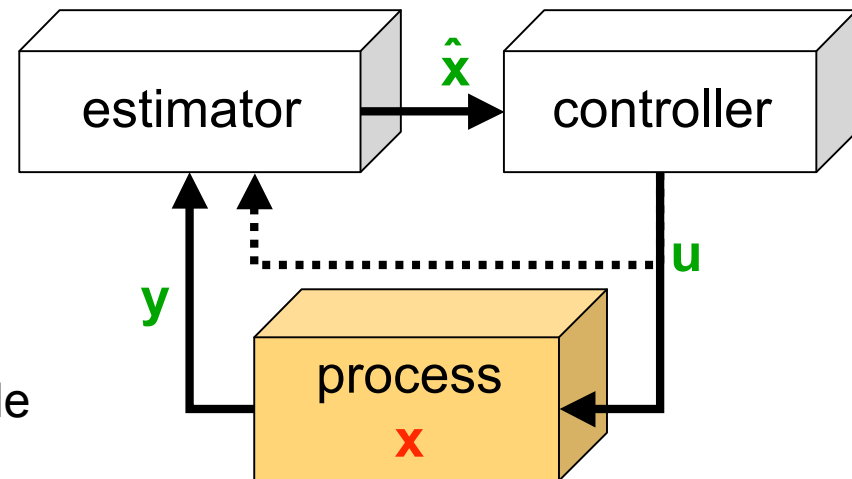
# Thank you!

Publications available at  
<http://www.info.ucl.ac.be/~pecheur/publi/>

# Backup Slides

# Process Control

- **Partially observable** process (hidden state  $\mathbf{x}$ , estimated by  $\hat{\mathbf{x}}$ )
- **observability** : infer  $\mathbf{x}$  from  $\mathbf{y}$  (and  $\mathbf{u}$ )
- **commandability** : impose  $\mathbf{x}$  through  $\mathbf{u}$
- **control theory** :  $\mathbf{x}$  = physical quantities, differentiable  
→ linear models, PDI controllers
- **logic processes** :  $\mathbf{x}$  = states, modes, **failures**, discrete  
→ state machines, programmable automata



# Verification of Control Systems

- **Monitors** and **commands** a process
  - in particular, **failure diagnosis** and **recovery**
- **Complex**
  - multiple controllers, asynchronism, coupling
  - race conditions, feature interaction
- **Software**
  - powerful and flexible but not linear, not continuous
- **How to Validate ?**
  - including "**diagnosability**" and "**recoverability**" from failures ?



# Temporal Epistemic Logic

- Reasoning about time and knowledge: **CTLK** logic

$$\begin{array}{l} \varphi ::= p \mid \neg\varphi \mid \varphi \wedge \varphi \qquad \text{atomic propositions, boolean ops} \\ \quad \mid EX \varphi \mid E[\varphi \text{ U } \varphi] \mid EG \varphi \qquad \text{temporal ops} \\ \quad \mid K_a \varphi \mid E_G \varphi \mid D_G \varphi \mid C_G \varphi \qquad \text{knowledge ops} \end{array}$$

with  $\varphi \vee \varphi' := \neg(\neg\varphi \wedge \neg\varphi')$ ,  $EF \varphi := E[\text{true U } \varphi]$ ,  $AG \varphi := \neg EF \neg\varphi$ , ...

- Interpreted over an *Interpreted System* =

- *Transition system* (Kripke structure)  $T +$
- *Observation functions*  $\text{obs}_a(\sigma)$  over runs  $\sigma$  of  $T$ , for each agent  $a$

$$\sigma \sim_a \sigma' \text{ iff } \text{obs}_a(\sigma) = \text{obs}_a(\sigma')$$

$$\sigma \models K_a \varphi \text{ iff for all } \underline{\text{reachable}} \sigma' . \sigma \sim_a \sigma' \Rightarrow \sigma' \models \varphi$$

# CTLK + correctness

$K_a^G \varphi$  = a knows  $\varphi$ , assuming everyone in G "works correctly"

- "works correctly" is a state condition
- Useful for diagnosis: one agent per component, works correctly iff non-fault mode
- Verification supported by Raimondi's tool (BDD based)
- Expressivity issue: correctness in present state vs. in future
- Work in progress!

# TO DO

- Full content
- Add references
  - Diagnosability
  - MC of CTLK
  - MC of Actions