



Model Checking for Software

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Credits

• Based on:







Menu

- Part I Explicit State Model Checking
 - What is model checking?
 - Kripke structures, temporal logic
 - Automata-theoretic model checking
 - Partial-order reduction, abstraction
 - Model Checking Programs: Java PathFinder
- Part II Symbolic Model Checking
 - Principles: BDDs
 - Tools: SMV
 - Application: model-based diagnosis





Part I Explicit State Model Checking





Part I

Explicit State Model Checking

- What is model checking?
- Kripke structures
 - Describing the systems we want to check
- Temporal logic
 - Describing the properties we want to check
- Automata-theoretic model checking
- State-explosion problem
 - What can we do?
- Model Checking Programs
 - A brief history of the field
 - Java PathFinder



Model Checking

- Model checking = (ideally) exhaustive exploration of the (finite) state space of a system
 - \approx exhaustive testing with loop / join detection







Model Checking The Intuition

- Calculate whether a system satisfies a certain behavioral property:
 - Is the system deadlock free?
 - Whenever a packet is sent will it eventually be received?
- Testing?
 - Look at all possible behaviors of a system
- Automatic, if the system is finite-state
 - Potential for being a push-button technology
 - Almost no expert knowledge required
- How do we describe the system?
- How do we express the properties?





Kripke Structures

- $K = (props, S, R, S_0, L)$
 - props : (finite) set of atomic propositions
 - -S: (finite) set of states
 - R: binary transitive relation (total)
 - S_0 : set of initial states
 - L: maps each state to the set of propositions true in the state
- Often M = (S,R,L) with props and S_0 implicit





Example Kripke Structure



 $K = (\{p, \ p\}, \{x, y, z, k, h\}, R, \{x\}, L)$

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Property Specifications

Temporal Logic

- Express properties of event orderings in time

- Linear Time
 - Every moment has a unique successor
 - Infinite sequences (words)
 - Linear Time Temporal Logic (LTL)



- Branching Time
 - Every moment has several successors
 - Infinite tree
 - Computation Tree Logic (CTL)







CTL*

- **State** formulae:
 - S ::= true | false | q | \sim q | S v S | S \wedge S | <u>A</u>P | <u>E</u>P
 - -A (for all) and E (there exists) are **path quantifiers**
- Path formulae:

 $P ::= S | P \vee P | P \wedge P | \sim P | XP | P U P$

- X (next), U (until) are **path operators**
- also: $\diamond p = Fp = \text{true } U p \text{ (finally, future)}$ $\Box p = Gp = \sim F \sim p \text{ (globally, always)}$ $\diamond p = Xp$

- Example:
$$A [F \text{ done } \lor F \text{ (failed } \land F \text{ done)}]$$





CTL and LTL

- **CTL**: Every path operator is preceded by a path quantifier (*AX*, *EX*, *A*(. *U*.), ...)
 - For example: AG(stuck => EF ~stuck)
- **LTL**: pure path formula *P*
 - No path quantifier, implicitly AP
 - For example: (A) (GF run => F done)





CTL



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- Two-process mutual exclusion with shared semaphore
- Each process has three states
 - Non-critical (N)
 - Trying (T)
 - Critical (C)
- Semaphore can be available (S_0) or taken (S_1)
- Initially both processes are in the Non-critical state and the semaphore is available --- $N_1 N_2 S_0$







- Mutual Exclusion: K \models AG ~(C₁ \land C₂)
- Response : K $\not\models$ AG $(T_1 \rightarrow AF(C_1))$
- Reactive : K \models AG EF (N₁ \land N₂ \land S₀)







 $K \models AG EF (N_1 \land N_2 \land S_0)$







 $K \models AG EF (N_1 \land N_2 \land S_0)$















































Model Checking

- Given
 - a Kripke structure $M = (props, S, R, S_0, L)$ that represents a finite-state concurrent system
 - a temporal logic formula *f* expressing some desired specification,
 - find the set of states in *S* that satisfy *f*: $[[f]] = \{ s \in S \mid M, s \models f \}$
- *M* satisfies *f* when all the initial states are in the set: $M \models f$ iff $S_0 \subseteq [[f]]$





Ing. Verification on d Evolution of Software Model Checking Complexity $M \models f$

- CTL
 - $\mathrm{O}(|M| * |f|)$
- LTL
 - $O(|M| * 2^{|f|})$
- But, for CTL the whole transition relation must be kept in memory!
 - Binary Decision Diagrams (BDDs) often allows the transition relation to be encoded efficiently
- The formulas are seldom very complex, hence |*f*| is not too troublesome.





Automata-Theoretic Model Checking

- Linear time temporal logic
 - Nondeterministic automata over infinite words
- Branching time temporal logic
 - Alternating automata over infinite trees
- Automata-theoretic LTL model checking
- Basic idea:
 - Translate both Kripke structure and LTL property into automata and show language containment
- See papers by <u>Vardi</u> and <u>Wolper</u>





Büchi Automata

- Accepts infinite words
- $B = (\sum, S, \rho, s_0, F)$
 - $-\sum$ is a finite alphabet
 - S is a finite set of states
 - $-\rho: S \times \Sigma \rightarrow 2^{S}$ is the transition function
 - $s_0 \in S$ is the initial state (or states)
 - $F \subseteq S$ is the set of accepting states
- Given an infinite word ω=a₀,a₁,... over ∑ then a *run* of B is the sequence s₀,s₁,...where s_{i+1} ∈ ρ(s_i, a_i)
- Let $inf(\pi)$ be the set of states that occur infinitely often on the run π , then π is accepting *iff inf* $(\pi) \cap F \neq \emptyset$





Example Büchi Automaton

$$B = (\{\{p\}, \{\sim p\}\}, \{1, 2\}, \rho, 1, \{2\})$$



Example accepting words:

- (12)^ω
- 1112^ω
- Example rejecting word: 121212111^ω
- LTL property: GFp "infinitely often p"





Kripke to Büchi Automaton

- $K = (props, S, R, S_0, L)$ can be viewed as
- $A_{K} = (2^{props}, S, \rho, S_{0}, S)$ where - $s_{i+1} \in \rho(s_{i}, a)$ *iff* $(s_{i}, s_{i+1}) \in R$ and a = L(s)
- Every state is in the accepting set, hence all runs are accepting
- The language of the automaton, $\mathcal{L}(A_K)$, is the set of all behaviors of K





Kripke to Büchi Example







Kripke to Büchi Example







Translating LTL Formulas to Büchi Automata

- Exponential in the length of the formula
 - Many heuristic optimizations are used
 - Multitude of papers: CAV, LICS, etc.







Model Checking with Büchi Automata

- K **|** f
- Translate K and f to Büchi Automata
- Language containment

$$- \mathcal{L}(A_{K}) \subseteq \mathcal{L}(A_{f})$$

$$- \mathcal{L}(A_{K}) \cap \overline{\mathcal{L}(A_{f})} = \emptyset$$

$$- \overline{\mathcal{L}(A_{f})} = \mathcal{L}(A_{\sim f}) \text{ and } \mathcal{L}(A_{K} \times A_{\sim f}) = \mathcal{L}(A_{K}) \cap \mathcal{L}(A_{\sim f})$$

- Algorithm
 - Negate formula f and create $A_{\sim f}$
 - Construct the product $A_{K,\sim f} = A_K \times A_{\sim f}$
 - If $\mathcal{L}(A_{K,\sim f}) = \emptyset$ report YES else report NO





Model Checking Example

- K **|** AFG~p
 - For all paths from some moment onwards p is always false

• Where K is given by

K)

h)

~p

p

~p





Step 1

- Negate FG~p
 - -GFp
- Construct Büchi Automaton for GFp






Step 2

• Construct the product automaton







Step 3



- Check if the language is empty
- It is nonempty since there is a cycle through an accepting state, hence K \ AFG~p
 - (xkhz)^{ω} is an accepting run
- The accepting run is also a counter-example to the property being true





Checking Nonemptiness

- A Büchi automaton accepts some word *iff* there exists an accepting state reachable from the initial state and from itself
- Can be checked in linear time
- Model Checking complexity for LTL
 O(|K| * 2^{|fl})





Efficient Nonemptiness Checking

Dfs (state s) Add (s,0) to VisitedStates; FOR each successor t of s DO IF (t,0) \notin VisitedStates THEN Dfs(t) END END IF s \in F THEN seed := s; 2Dfs(s) END END

```
2Dfs (state s)

Add (s,1) to VisitedStates;

FOR each successor t of s DO

IF (t,1) \notinVisitedStates THEN 2Dfs(t) END

ELSEIF t = seed THEN report nonempty END

END

END
```

Efficiency

- VisitedStates as HashTable
- Change Recursion to Iteration
- Generate successor states on-the-fly





SPIN Model Checker

- Automata based model checker
 - Efficient nonemptiness algorithm
- Translates LTL formula to Büchi automaton
- Kripke structures are described as "programs" in the PROMELA language
 - Kripke structure is generated on-the-fly during nonemptiness checking
- <u>http://spinroot.com</u>
 - Relevant theoretical papers can be found here





State-space Explosion?

- n concurrent processes with m states each
 - Has mⁿ states
 - Worst-case, an on-the-fly model checker has to enumerate all of them
- What can we do to reduce mⁿ?
 - Reduce m
 - Abstraction
 - Reduce the effect of n
 - Partial-order reductions
 - Reduce n
 - Symmetry reductions

We'll consider these 2 here





Partial-Order Reductions

- Reduce the number of interleavings of independent concurrent transitions
- $\mathbf{x} := 1 \parallel \mathbf{y} := 1$ where initially $\mathbf{x} = \mathbf{y} = 0$







Basic Ideas

- Independent transitions
 - cannot disable nor enable each other
 - are **commutative**
- Partial-order reductions only apply during the on-the-fly construction of the Kripke structure
- Based on a selective search principle
 - Execute a subset of enabled transitions in a state
- Sleep sets (reduce transitions)
- **Persistent sets**, ample sets (reduce states)





Persistent Set

Given a set of transitions \sum and a state s,

 T ⊆ enabled(s) ⊆ ∑ is persistent in s iff on any execution in (∑–T) from s, all transitions are independent from all transitions in T







Persistent Set Reductions

- Use the **static structure** of the system to determine **sufficient conditions** for persistent sets
 - Note, the set of **all enabled transitions** is trivially persistent
- Only execute transitions in the persistent set
- Persistent set algorithm is used within SPIN
- See papers by <u>Godefroid</u> and <u>Peled</u>





Abstraction

- Type-based abstractions
 - Abstract Interpretation
 - Replace concrete variables with abstract variables
 - E.g. integer with {odd, even} real with {neg, zero, pos}
 - ... and concrete operations with abstract operations
 - e.g. add(pos,pos) = possubtract(pos,pos) = neg | zero | poseq(pos,pos) = true | false
- Predicate Abstraction (<u>Graf</u>, <u>Saïdi</u> see also <u>Uribe</u>)
 - Create abstract state-space w.r.t. set of predicates defined in concrete system





Predicate Abstraction



- Mapping of a concrete system to an abstract system, whose states correspond to truth values of a set of predicate
- Create abstract state-graph during model checking, or,
- Create an abstract transition system before model checking





Model Checking Programs

- Model checking usually applied to **designs**
 - + More abstract, smaller, earlier
 - Some errors get introduced after designs
 - Design errors are missed due to lack of detail
 - Sometimes there is no design
- Can model checking find errors in real programs?
 - Yes, many examples in the literature
- Can model checkers be used by programmers?
 - Only if it takes real programs as input





Main Issues

- Memory
 - Explicit-state model checking's Achilles heel
 - State of a software system can be complex
 - Require efficient encoding of state, or,
 - State-less model checking
- Input notation not supported
 - Translate to existing notation
 - Custom-made model checker
- State-space Explosion





State-less Model Checking

- Must limit search-depth to ensure termination
- Based on partial-order reduction techniques
- Annotate code to allow verifier to detect "important" transitions
- Example: VeriSoft http://cm.bell-labs.com/who/god/verisoft/





Traditional Model Checking

- Translation-based using existing model checker
 - Hand-translation
 - Semi-automatic translation
 - Fully automatic translation
- Custom-made model checker
 - Fully automatic translation
 - More flexible





Hand-Translation



- Hand translation of program to model checker's input notation
- "Meat-axe" approach to abstraction
- Labor intensive and error-prone





Hand-Translation Examples

- Remote Agent Havelund, Penix, Lowry 1997
 - <u>http://ase.arc.nasa.gov/havelund</u>
 - Translation from Lisp to Promela (most effort)
 - Heavy abstraction
 - 3 man months
- DEOS Penix *et al.* 1998/1999
 - <u>http://ase.arc.nasa.gov/visser</u>
 - C++ to Promela (most effort in environment)
 - Limited abstraction programmers produced sliced system
 - 3 man months





Semi-Automatic Translation

- Table-driven translation and abstraction
 - Feaver system by Gerard Holzmann
 - User specifies code fragments in C and how to translate them to Promela (SPIN)
 - Translation is then automatic
 - Found 75 errors in Lucent's PathStar system
 - <u>http://cm.bell-labs.com/cm/cs/who/gerard/</u>
- Advantages
 - Can be reused when program changes
 - Works well for programs with long development and only local changes





Fully Automatic Translation

- Advantage
 - No human intervention required
- Disadvantage
 - Limited by capabilities of target system
- Examples
 - Java PathFinder 1- <u>http://ase.arc.nasa.gov/havelund/jpf.html</u>
 - Translates from Java to Promela (Spin)
 - JCAT <u>http://www.dai-arc.polito.it/dai-arc/auto/tools/tool6.shtml</u>
 - Translates from Java to Promela (or dSpin)
 - Bandera <u>http://www.cis.ksu.edu/santos/bandera/</u>
 - Translates from Java bytecode to Promela, SMV or dSpin





Custom-made Model Checkers

- Allows efficient model checking
 - Often no translation is required
 - Algorithms can be tailored
- Translation-based approaches
 - dSpin
 - Spin extended with dynamic constructs
 - Essentially a C model checker
 - <u>http://www.dai-arc.polito.it/dai-arc/auto/tools/tool7.shtml</u>
 - Java Model Checker (from Stanford)
 - Translates Java bytecode to SAL language
 - Custom-made SAL model checker
 - <u>http://sprout.stanford.edu/uli/</u>





Java PathFinder

- Explicit-state model checking
- Build own Java Virtual Machine
 - Emphasis on memory management not speed
 - Bytecode level assures language coverage
- Written in Java
 - 1 month to develop version with only integers
- Efficient encoding of states
 - Canonical heap representation
- Modular design to allow flexible system
 - Different search algorithms, listeners, heuristics, ...





JPF Current Status



- "Today, JPF is a swiss army knife for all sort of runtime based verification purposes"
- http://javapathfinder.sourceforge.net/





Part II Symbolic Model Checking





Part II Symbolic Model Checking

- Principles
 - BDDs
 - Symbolic MC algorithm
- Tools: *SMV*
 - Principles, Language, Variants
- Application:
 - Livingstone model-based diagnosis

Some material from Edmund Clarke and Marius Minea





Symbolic Model Checking Principles





Instead of considering each individual state,

Symbolic model checking...







Instead of considering each individual state,

Symbolic model checking...

• Manipulates sets of states,







Instead of considering each individual state,

Symbolic model checking...

- Manipulates sets of states,
- Represented as boolean formulas,







Instead of considering each individual state, Symbolic model checking... 0^{0}

- Manipulates sets of states,
- Represented as boolean formulas,



• Encoded as binary decision diagrams.





Instead of considering each individual state, Symbolic model checking... 0^{0}

- Manipulates sets of states,
 - Can handle very large state spaces $(10^{50} +)^{\psi}_{y}$
- Represented as boolean formulas,
 - Suited for boolean/abstract models
- Encoded as binary decision diagrams.
 The limit is BDD size (hard to control)







Boolean Functions

• Represent a state as boolean variables

$$s = b_1, ..., b_n$$

Non-boolean variables => use boolean encoding

- A set of states as a boolean function $s \text{ in } S \text{ iff } f(b_1, ..., b_n) = 1$
- A transition relation as a boolean function over two states

$$s \rightarrow s'$$
 iff $f(b_1, ..., b_n, b'_1, ..., b'_n) = 1$





Binary Decision Trees

- Encoding for boolean functions
- Notational convention: = if c then e else e' = (c ? e : e')



 $(a \mid b) \Longrightarrow c$

• Always exists but not unique





From Trees to Diagrams

- Fixed variable ordering
 - "layered" tree



 $(a \mid b) \Longrightarrow c$





From Trees to Diagrams

- Fixed variable ordering "layered" tree
- Merge equal subtrees



 $(a \mid b) \Longrightarrow c$





From Trees to Diagrams

- Fixed variable ordering "layered" tree
- Merge equal subtrees
- Remove nodes with equal subtrees



 $(a \mid b) \Longrightarrow c$

=> Ordered Binary Decision Diagram




[Ordered] Binary Decision Diagrams

- [O]BDDS for short
- Unique normal form
 - for a given ordering and
 - up to isomorphism
 - => compare in constant time (using hash table)



 $(a \mid b) \Longrightarrow c$





Computations with BDDs

• Negation !*f*:

swap leaves 0 and 1.

- Boolean combinator *f#g*:
 (b?f':f') # (b?g':g'') = (b?f'#g':f''#g'')
 cache results -> O(|f/./g/) time
- Instantiation *f*[*b*=1], *f*[*b*=0]:
 (b?f':f')[b=1] = f'
- Quantifiers exists *b* . *f*, forall *b* . *f* : exists *b* . *f* = *f*[*b*=1] | *f*[*b*=0]





Variable Ordering

- Must be the same for all BDDs
- Size of BDDs depends critically on ordering
- Worst case: exponential w.r.t. #variables
 - sometimes exponential for any ordering
 - e.g. middle output bit of n-bit multiplier
- Finding optimum is hard (NP-complete)
 => optimization uses heuristics





Transition Systems with BDDs

Given boolean state variables $v = b_1, ..., b_n$ a set of states as a BDD p(v)

a transition relation as a BDD T(v, v')

we can compute the predecessors and successors of *p* as BDDs:

 $(pred p)(v) = exists v' \cdot T(v, v') \& p(v')$ $(succ p)(v) = exists v' \cdot p(v') \& T(v', v)$







Checking Formulas with BDDs

Functional evaluation as set of states:

- for every formula *p*, build the BDD *p*(*v*)
 of the set of states that satisfy *p*
- Top level: for a set of initial states *I*,

I satisfy *p* iff !p & I = 0

• $p = op(q,r) \Longrightarrow$ build p(v) based on q(v), r(v)





CTL temporal logic



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CTL operators as BDDs

 $(\mathbf{EX} \ p)(v) = (\mathbf{pred} \ p)(v) = \mathbf{exists} \ v' \cdot T(v, v') \& \ p(v')$ $(\mathbf{EG} \ p)(v) = (\mathbf{gfp} \ U \cdot p \& \mathbf{EX} \ U)(v)$ $(\mathbf{E}[p \ \mathbf{U} \ q])(v) = (\mathbf{lfp} \ U \cdot q \mid (p \& \mathbf{EX} \ U))(v)$

All others can be expressed as EX/EG/EU

EF
$$p = \mathbf{E}[1 \mathbf{U} p]$$

AX $p = !\mathbf{EX} ! p$
AG $p = !\mathbf{EF} ! p$
AF $p = !\mathbf{EG} ! p$
A[$p \mathbf{U} q$] = !**E**[! $q \mathbf{U} ! p \& !q$] & !**EG** ! q



. . .



Evaluating Fixpoints with BDDS

Compute **lfp** $U \cdot F[U]$ as a BDD: $U_{0}(v) = 0$

$$U_1(v) = F[U_0](v) = F[0](v)$$

 $U_{n+1}(v) = F[U_n](v) = F^n[0](v)$



until $U_n(v) = U_{n+1}(v) = (\mathbf{lfp} \ U \ . \ F[U])(v)$

Convergence assured because finite domain

– Dual construction for **gfp**

























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Fairness, LTL

- CTL+fairness:
 - Only check executions where fairness conditions $c_1, ..., c_n$ hold infinitely often
 - Symbolic evaluation: express $c_1, ..., c_n$ as BDDs, modified algorithms for **EX**, **EG**, **EU**.
- Symbolic model checking of LTL
 - Convert LTL formula to Büchi automaton
 - Encode automaton in transition relation
 - Express acceptance condition in CTL+fairness





Bounded Model Checking

- Principle:
 - n+1 copies of state variables $v_0, ..., v_n$
 - Unroll transition relation *n* times $T(v_{k-1}, v_k)$
 - Embed property to be satisfied
 - Verify satisfiability with SAT procedure
- Verifies traces up to length *n*
 - Iterate over values of n => breadth-first search
- No state space explosion (polynomial space)
- Usually fast (though worst case is exponential time)





Symbolic Model Checking Summary

- Principle: compute over sets of states encoded as BDDs.
- Can handle huge state spaces.
- CTL + fairness, LTL.
- Some tweaking may be needed.
 - variable ordering
- Some models blow up nevertheless.
- New alternative: **SAT-based** (bounded).





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Verifying LTL using symbolic model checking.





Symbolic Model Checking Tools: SMV





Overview

- **SMV** = **S**ymbolic **M**odel **V**erifier.
- Developed by Ken McMillan at Carnegie Mellon University.
- Modeling language for transition systems based on parallel assignments.
- Specifications in temporal logic CTL.
- BDD-based symbolic model checking: can handle very large state spaces.





What SMV Does







SMV Program Example (1/2)

```
MODULE user(turn, id, other)
VAR state: {n, t, c};
DEFINE my turn :=
   (other=n) | ((other=t) & (turn=id));
ASSTGN
init(state) := n;
next(state) := case
   (state = n) : \{n, t\};
                                   t )!my_turn
   (state = t) & my turn: c;
                                    my turn
   (state = c) : n;
   1 : state;
esac;
```

SPEC AG((state = t) \rightarrow AF (state = c))





SMV Program Example (2/2)

```
MODULE main
VAR turn: {1, 2};
    user1: user(turn, 1, user2.state);
    user2: user(turn, 2, user1.state);
ASSTGN
init(turn) := 1;
next(turn) := case
   (user1.state=n) & (user2.state=t): 2;
   (user2.state=n) & (user1.state=t): 1;
   1: turn;
esac;
SPEC AG !((user1.state=c) &
  (user2.state=c))
```

```
SPEC AG ! (user1.state=c)
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```





Diagnostic Trace Example

- -- specification AG (state = t -> AF state = c) (in module user1) is true
- -- specification AG (state = t -> AF state = c) (in module user2) is true
- -- specification AG (!(user1.state = c & user2.state =
 c)... is true
- -- specification AG (!user1.state = c) is false
- -- as demonstrated by the following execution sequence state 1.1:

```
turn = 1
```

```
user1.state = n
user2.state = n
```

```
state 1.2:
user1.state = t
```

state 1.3:
user1.state = c





The Essence of SMV

- The SMV program defines:
 - a finite transition model M (Kripke structure),
 - a set of possible initial states *I* (may be several),

- specifications $P_1 \dots P_m$ (CTL formulas).

• For each specification *P*, SMV checks that $\forall s_o \in I \ . \ M, s_o \models P$

Note: **SPEC** IP is not the negation of **SPEC** P: both can be false (in some initial states), both can be true (vacuously when $I=\emptyset$).





Variables and Transitions (Assignment Style)

```
VAR state: {n, t, c};
ASSIGN
init(state) := n;
next(state) := case
  (state = n) : {n, t}; ...
esac;
```

- Finite data types (incl. numbers and arrays).
- Usual operations x&y, x+y, etc., case statement.
- All assignments are evaluated in parallel.
- No control flow (must be simulated with vars).
- SMV detects circular and duplicate assignments.





Modules

```
MODULE user(turn,id,other)
VAR ...
ASSIGN ...
MODULE main
VAR user1: user(turn,1,user2.state);
...
```

- Parameters passed by reference.
- Top-level module main.
- Composition is synchronous by default: all modules move at each step.





Processes

VAR node1: process node(1);
node2: process node(2);

- Composition of processes is asynchronous: one process moves at each step.
- Boolean variable running in each process
 - running=1 when that process is selected to run.
 - Used for fairness constraints (see later).





Fairness

```
MODULE user(turn,id,other)
VAR ...
ASSIGN ...
SPEC AG AF (state = c)
FAIRNESS (state = t)
```



- Check specifications, assuming fairness conditions hold repeatedly (infinitely often).
- Useful for liveness properties.
- Fair scheduling: FAIRNESS running





Variables and Transitions (Constraint Style)

VAR pos: {0,1,2,3,4,5}; INIT pos < 2 TRANS (next(pos)-pos) in {+2,-1} INVAR !(pos=3)

- Any propositional formula is allowed
 => flexible for translation from other languages.
- INVAR p is equivalent to INIT p TRANS next(p) but implemented more efficiently.
- Risk of inconsistent models (TRANS p & !p).





Well-Formed Programs?

- In assignment style, by construction:
 - always at least one initial state,
 - all states have at least one next state,
 - non-determinism is apparent (unassigned variables, set assignments, interleaving).
- In constraint style:
 - INIT and TRANS constraints can be inconsistent,
 - the level of non-determinism is emergent from the conjunction of all constraints.





Variable Ordering

- BDDs require a fixed variable ordering.
 - Critical for performance (BDD size).
 - Best one is hard to find (NP-complete).
- SMV does not optimize by default but
 - can read, write ordering in a file,
 - can search for better ordering on demand.





NuSMV

- From ITC-IRST (Trento, Italy) and CMU.
- New version of SMV, completely rewritten:
 - Same language as SMV.
 - Modular, documented APIs, easily customized.
 - Specifications in CTL or LTL.
 - Graphical User Interface.
- See http://nusmv.irst.itc.it/





Related Tools

- Cadence SMV (Cadence Berkeley Labs)
 - From Ken McMillan, original author of SMV.
 - Supports refinement, compositional verification.
 - New language but accepts CMU SMV.
 - see <u>http://www-cad.eecs.berkeley.edu/~kenmcmil/smv/</u>

• Bounded Model-Checking

- Based on SAT solvers
- Bounded verification
- Checks LTL formulae (=> Büchi automata)
- Part of NuSMV





SMV Summary

- BDD-based symbolic model checker.
- Modeling language based on synchronous transition systems.
- Constraint style: more versatile, less strict
 => good for use as back-end tool.
- 1st generation: CMU
- 2nd generation: Cadence, NuSMV
- Variant: **BMC** (SAT based)





SMV References

Ken McMillan. Symbolic Model Checking. Kluwer Academic Publishers, 1993.

Based on Ken McMillan's PhD thesis on SMV.

- Ken L. McMillan. The SMV System (draft). February 1992. <u>http://www.cs.cmu.edu/~modelcheck/smv/smvmanual.r2.2.ps</u> *The (old) user manual provided with the SMV program.*
- A. Cimatti, E. Clarke, F. Giunchiglia, and M. Roveri. NuSMV: A New Symbolic Model Verifier. In N. Halbwachs and D. Peled, eds., Proceedings of International Conference on Computer-Aided Verification (CAV'99), LNCS 1633:495-499, Springer Verlag. Survey paper on NuSMV.





Symbolic Model Checking Applications in Software




Applications of Symbolic Model Checking

- Used in industry for hardware design
 - Commercial tools (Cadence)
 - Fits well with boolean modeling
- Some success stories in protocol design
 - Cache coherence of IEEE Futurebus+
 - HDLC
- Not so good for software design
 - Gap between programming/design language and verification modeling language.





Model-Based Autonomy

- Unattended control of a complex device (e.g. a spacecraft)
- Based on AI technology
- General reasoning engine + application-specific model
- Use model to respond to unanticipated situations



=> Verify the model !





The Livingstone Diagnostic System

- Mode identification & recovery:
 - identify current state (including faults)
 - find path to goal state
- Model-based
- From NASA Ames
- Run in space (DS- 1, May 1999)







Verification of Autonomy Models







Livingstone Models

- Models = concurrent transition systems
- Qualitative values
 => finite state
- Nominal/fault modes **Closed**
- Probabilities on faults



Courtesy Autonomous Systems Group, NASA Ames





Application In-Situ Propellant Production

- Use atmosphere from Mars to make fuel for return flight.
- Livingstone controller developed at NASA Kennedy.
- Components are tanks, reactors, valves, sensors...
- Exposed improper flow modeling.
- Very "loose" state space:
 - -10^{50} states
 - all states reachable in 3 steps

Mars
atmosphere on-board

$$CO_2 + 2H_2 \longrightarrow CH_4 + O_2$$

fuel oxidizer





Verification of Diagnosability





- Intuition: bad is diagnosable if and only if there is no pair of trajectories, one reaching a bad state, the other reaching a good state, with identical observations.
 - or some generalization of that: (context, two different faults, ...)
- Principle:
 - consider two concurrent copies x1, x2 of the process,
 with coupled inputs u and outputs y
 - check for reachability of (good(x1) && bad(x2))
- Back to a classical (symbolic) model checking problem !
- Supported by Livingstone-to-SMV translator



Application: X-34 / PITEX

- Propulsion IVHM Technology Experiment (ARC, GRC)
- Livingstone applied to propulsion feed system of space vehicle
- Livingstone model is 4.10³³ states
- Found impossible diagnosis of stuck venting valve







Applications of SMV Summary

- Symbolic model checking:
 OK for hardware, quid for software?
- Needs translation from programming language to verification language and back!
- 2 examples for autonomy software using SMV.





Applications of SMV References

C. Pecheur and R. Simmons. "From Livingstone to SMV: Formal Verification for Autonomous Spacecrafts". *First Goddard Workshop on Formal Approaches to Agent-Based Systems*, NASA Goddard, April 5-7, 2000.

Verification of Livingstone with SMV.

R. Simmons and C. Pecheur. "Automating Model Checking for Autonomous Systems". *AAAI Spring Symposium on Real-Time Autonomous Systems*, Stanford CA, March 2000.

Verification of TDL with SMV.